

Algorithm Design
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Solution of Exercise R-4.16

No. Bucket-sort does not use a constant amount of additional storage. It uses $O(n + N)$ space.